

2. [Maximum mark: 4]

A company that owns many restaurants wants to determine if there are differences in the quality of the food cooked for three different meals: breakfast, lunch and dinner.

Their quality assurance team randomly selects 500 items of food to inspect. The quality of this food is classified as perfect, satisfactory, or poor. The data is summarized in the following table.

		Quality			Total
		Perfect	Satisfactory	Poor	
Meal	Breakfast	101	124	7	232
	Lunch	68	81	5	154
	Dinner	35	69	10	114
Total		204	274	22	500

A χ^2 test at the 5% significance level is carried out to determine if there is significant evidence of a difference in the quality of the food cooked for the three meals.

The critical value for this test is 9.488.

The hypotheses for this test are:

H_0 : The quality of the food and the type of meal are independent.

H_1 : The quality of the food and the type of meal are not independent.

(a) Find the χ^2 statistic.

[2]

(b) State, with justification, the conclusion for this test.

[2]

(This question continues on the following page)

9. [Maximum mark: 9]

At a running club, Sung-Jin conducts a test to determine if there is any association between an athlete's age and their best time taken to run 100m. Eight athletes are chosen at random, and their details are shown below.

Athlete	A	B	C	D	E	F	G	H
Age (years)	13	17	22	18	19	25	11	36
Time (seconds)	13.4	14.6	13.4	12.9	12.0	11.8	17.0	13.1

Sung-Jin decides to calculate the Spearman's rank correlation coefficient for his set of data.

- (a) Complete the table of ranks. [2]

Athlete	A	B	C	D	E	F	G	H
Age rank			3					
Time rank							1	

- (b) Calculate the Spearman's rank correlation coefficient, r_s . [2]
- (c) Interpret this value of r_s in the context of the question. [1]
- (d) Suggest a mathematical reason why Sung-Jin may have decided not to use Pearson's product-moment correlation coefficient with his data from the original table. [1]
- (e) (i) Find the coefficient of determination for the data from the original table.
- (ii) Interpret this value in the context of the question. [3]

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10. [Maximum mark: 6]

A chocolate company plans to produce chocolate bars with special flavours. They survey 246 people to determine if there is any particular preference for one of the flavours.

The table below shows the information collected.

Hot chilli	Almond crunch	Spiced Chai	Ginger'n'lime
75	59	46	66

A χ^2 goodness of fit test at the 5% significance level is carried out on the data.

The critical value for the test is 7.82.

- (a) State the null and alternative hypotheses for this test.
- (b) Perform the test and give your conclusion in context.

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11.



11. [Maximum mark: 6]

Two AC (alternating current) electrical sources of equal frequencies are combined.

The voltage of the first source is modelled by the equation $V = 30 \sin(t + 60^\circ)$.

The voltage of the second source is modelled by the equation $V = 60 \sin(t + 10^\circ)$.

(a) Determine the maximum voltage of the combined sources. [2]

(b) Using your graphic display calculator, find a suitable equation for the combined voltages, giving your answer in the form $V = V_0 \sin(at + b)$, where a , b and V_0 are constants, $a > 0$ and $0^\circ \leq b < 180^\circ$. [4]

Large empty rectangular box for student work, containing horizontal dotted lines for writing.

[2]

[4]



13. [Maximum mark: 7]

The matrices $P = \begin{pmatrix} 3 & 1 \\ 0 & 2 \end{pmatrix}$ and $Q = \begin{pmatrix} -4 & 1 \\ 1 & 3 \end{pmatrix}$ represent two transformations.

A triangle T is transformed by P , and this image is then transformed by Q to form a new triangle, T' .

- (a) Find the single matrix that represents the transformation $T' \rightarrow T$, which will undo the transformation described above.

[4]

The area of T' is 273 cm^2 .

- (b) Using your answer to part (a), or otherwise, determine the area of T .

[3]

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14. [Maximum mark: 8]

In this question, i denotes a unit vector due east, and j denotes a unit vector due north.

Two ships, A and B, are each moving with constant velocities.

The position vector of ship A, at time t hours, is given as $r_A = (1 + 2t)i + (3 - 3t)j$.

The position vector of ship B, at time t hours, is given as $r_B = (-2 + 4t)i + (-4 + t)j$.

- (a) Find the bearing on which ship A is sailing. [3]
- (b) Find the value of t when ship B is directly south of ship A. [2]
- (c) Find the value of t when ship B is directly south-east of ship A. [3]

A large rectangular area containing horizontal dotted lines for writing answers.

15. [Maximum mark: 6]

A random sample of eight packets of Apollo coffee granules are selected from a supermarket shelf.

The weights of the coffee granules present in each packet are as follows:

222 g 226 g 221 g 228 g 227 g 225 g 222 g 223 g

- (a) (i) Find an unbiased estimate for the mean weight of coffee granules in a packet of Apollo coffee. [3]
- (ii) Calculate a 95% confidence interval for the population mean. Give your answer to four significant figures. [1]
- (b) State one assumption you have made in order for your interval to be valid. [1]
- (c) The label of each packet has a description which includes the phrase: "contains 226 g of coffee granules". [2]

Using your answer to part (a)(ii), briefly comment on the claim on the label. [2]

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